Matching algorithms and superpixels for image analysis and processing

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Many domains, for many applications:



Goal: To automatically generate a result for an input data.

Segmentation and labeling example:



Goal: To automatically generate a result for an input data.

Segmentation and labeling example:

 \rightarrow Necessity to use a extern source of information.



Non-local patch-based methods:

Search for matches for each pixel (patch) of the input image.

example with ground truth



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• in a library of example images

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- in a library of example images
- without learning step

Non-local patch-based methods:

Search for matches for each pixel (patch) of the input image.



Stake n°1: To propose an algorithm that computes these matches:

- in a library of example images
- without learning step
- in a fast way

Data sometimes sizeable and high computational times.



3D volume



HD image



Video

Data sometimes sizeable and high computational times.

3D volume



HD image



Video

- \rightarrow Methods to reduce the resolution
 - Regular multi-resolution :

Decompose the image into regular blocks.







Decomposition into blocks



Average colors

Image

Data sometimes sizeable and high computational times.



3D volume

HD image

Video

- \rightarrow Methods to reduce the resolution
 - Superpixels (since [Ren and Malik, 2003]): Local grouping of pixels with homogeneous colors.



Image

Decomposition into superpixels

Data sometimes sizeable and high computational times.



3D volume

HD image

Video

- \rightarrow Methods to reduce the resolution
 - Superpixels (since [Ren and Malik, 2003]): Local grouping of pixels with homogeneous colors.



Image

Decomposition into superpixels

Average colors

Stake nº2: Irregularity of the decomposition.

 \rightarrow Limits their use into methods using neighborhood.





Matching algorithm based on patches of superpixels and applications

Decomposition into regular superpixels



Conclusion and perspectives





Matching algorithm based on patches for medical image segmentation

- Context
- State-of-the-art
- The OPAL method
- Segmentation results
- Conclusion

Matching algorithm based on patches of superpixels and applications

Decomposition into regular superpixels

5 Conclusion and perspectives

Context

- Cerebral images for neurodegenerative diseases (e.g., Alzheimer).
- Analysis of impacted structures necessary for patient follow-up. Manual segmentation very time consuming. High inter-expert variability.





 \rightarrow To propose automatic, precise and fast segmentation methods.

Context

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 \rightarrow To propose automatic, precise and fast segmentation methods.

State-of-the-art - Deformation methods

Computation of non-linear transformation. Deformation of the model's structure.

[Collins et al., 1995]

 \rightarrow Very important computational time (hours).



subject to segment

reference model with manual segmentation

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subject to segment

reference model with manual segmentation

Multi-template approach.

[Heckemann et al., 2006]



State-of-the-art - Patch-based method [Coupé et al., 2011]

Linear registration (minutes).

Weighted average of the model's patches in a restricted search area.





 \rightarrow Necessary preselection and high number of considered dissimilar patches. \rightarrow Computational time $\approx 10 \text{mn}$ by subject.

State-of-the-art - Patch-based method [Coupé et al., 2011]

Linear registration (minutes).

Weighted average of the model's patches in a restricted search area.





Proposition: To use a fast matching algorithm to compute several good matches within the models.

State-of-the-art - Matching algorithm

Choice of the PatchMatch algorithm [Barnes et al., 2009]: Computation of a match in B for each patch of A.



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Key idea: To use the information from adjacent patches to propagate good matches.



 \rightarrow The complexity of the algorithm only depends on the size of the image A.

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Weighted average of models patches in a restricted search area.





Proposition: To use a fast matching algorithm to compute several good matches within the models.









- \rightarrow Reduced number of patches contributing to the segmentation.
- \rightarrow No necessary preselection.
- \rightarrow Reduced computational time.

Independent multi-feature and multi-scale search and fusion.



 \rightarrow Increase of the segmentation process accuracy.

 $\begin{array}{l} \mbox{Validation metric [Zijdenbos et al., 1994]:} \\ \mbox{Dice}(\mathcal{S}_{\mbox{expert}}, \mathcal{S}_{\mbox{auto}}) = \frac{2|\mathcal{S}_{\mbox{expert}} \cap \mathcal{S}_{\mbox{auto}}|}{|\mathcal{S}_{\mbox{expert}}| + |\mathcal{S}_{\mbox{auto}}|} \\ \end{array}$

Segmentation results

 $\begin{aligned} & \text{Validation metric [Zijdenbos et al., 1994]:} \\ & \text{Dice}(\mathcal{S}_{\text{expert}}, \mathcal{S}_{\text{auto}}) = \frac{2|\mathcal{S}_{\text{expert}} \cap \mathcal{S}_{\text{auto}}|}{|\mathcal{S}_{\text{expert}}| + |\mathcal{S}_{\text{auto}}|} \end{aligned}$

 ICBM dataset: 80 young healthy subjects [Mazziotta et al., 1995] Inter-expert variability: 90%.

Method	Median Dice	Computational time
Patch-based [Coupé et al., 2011]	88.2%	$(\times 700)$
Multi-templates [Collins and Pruessner, 2010]	88.6%	$(\times 4300)$
Dictionary learning [Tong et al., 2013]	89.0%	$(\times 1000)$
OPAL (2015)	$\mathbf{90.0\%}$	0.92s

• EADC-ADNI: 100 healthy and unhealthy subjects [Boccardi et al., 2014] Inter-expert variability: 89%.

Method	Average Dice	Computational time
Random Forest [Tangaro et al., 2014]	76.0%	×
Multi-templates [Gray et al., 2014]	87.6%	×
Patch-based [Zhu et al., 2017]	88.3%	×
Multi-scale patch-based [Pant et al., 2015]	89.2%	$(\times 200)$
OPAL (2015)	$\mathbf{89.8\%}$	1.48s





Conclusion

- PatchMatch for a library of 3D images
- New automatic segmentation method
- Results > inter-expert variability in a few seconds

Associated publications:

- Vinh-Thong Ta, <u>Rémi Giraud</u>, D. Louis Collins, and Pierrick Coupé. Optimized PatchMatch for near real time and accurate label fusion. Proc. of Int. Conf. on Medical Image Computing and Computer-Assisted Intervention (MICCAI), pages 105–112, 2014.
- <u>Rémi Giraud</u>, Vinh-Thong Ta, Nicolas Papadakis, D. Louis Collins, and Pierrick Coupé. Optimisation de l'algorithme PatchMatch pour la segmentation de structures anatomiques. Actes du Groupe d'Etudes du Traitement du Signal et des Images (GRETSI), 2015.
- <u>Rémi Giraud</u>, Vinh-Thong Ta, Nicolas Papadakis, Jose V., Manjón, D. Louis Collins, and Pierrick Coupé. An optimized PatchMatch for multi-scale and multi-feature label fusion. NeuroImage (NIMG), 124:770–782, 2016.

Extensions of OPAL

- Extension to the cerebellum segmentation [Manjón et al., 2017] [Romero et al., 2017]
- Extension to the Alzheimer's disease prediction [Hett et al., 2016]
- Integration into the online platform volBrain [Manjón et Coupé, 2016]







Associated publications:

- Kilian Hett, Vinh-Thong Ta, <u>Rémi Giraud</u>, Mary Mondino, Jose V. Manjón, and Pierrick Coupé. Patch-based DTI grading: Application to alzheimer's disease classification. Proc. of Int. Work. on Patch-based Techniques in Medical Imaging (Patch-MI, MICCAI), pages 76–83, 2016.
- Jose V. Manjón, Pierrick Coupé, Jose E. Romero, Vinh-Thong Ta, and <u>Rémi Giraud</u>. Ceres: A new cerebellum lobule segmentation method. *Dépot logiciel : IDDN.FR.001.470008.000.S.P.2015.000.21000*, 2016.
- Jose E. Romero, Pierrick Coupé, <u>Rémi Giraud</u>, Vinh-Thong Ta, Vladimir Fonov, and Min Tae M. Park, et al. CERES: A new cerebellum lobule segmentation method. NeuroImage (NIMG), 147:916–924, 2017.
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- Jose V. Manjón, Pierrick Coupé, Jose E. Romero, Vinh-Thong Ta, and <u>Rémi Giraud</u>. Ceres: A new crebellum lobule segmentation method. Dépot logiciel : IDDN.FR.001.470008.000.5.P.2015.000.20100, 2016.
- Jose E. Romero, Pierrick Coupé, <u>Rémi Giraud</u>, Vinh-Thong Ta, Vladimir Fonov, and Min Tae M. Park, et al. CERES: A new cerebellum lobule segmentation method. *NeuroImage* (*NIMG*), 147:916–924, 2017.



2 Matching algorithm based on patches for medical image segmentation



Matching algorithm based on patches of superpixels and applications

- The SuperPatchMatch method
- Application to color transfer
- Superpatch
- Application to segmentation and labeling
- Conclusion





The SuperPatchMatch method

Adaptation of the PatchMatch algorithm to superpixels:

- Similar initialization and random search.
- Propagation: necessity to preserve the relative positions between adjacent neighbors.



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Adaptation of the PatchMatch algorithm to superpixels:

- Similar initialization and random search.
- Propagation: necessity to preserve the relative positions between adjacent neighbors.
 - \rightarrow Selection of the neighbor with the most similar orientation.



 \rightarrow SuperPatchMatch: fast search algorithm of superpixel-based matches.

Constraints:

- Reduced computational time (HD, video)
 - Global transfer of the source color palette
 - Respect of the target structures



Source image



Target image



Transfer result

Constraints: • Reduced computational time (HD, video)

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Superpixel-based Color Transfer (SCT):



Target image

Transfer result

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Superpixel-based Color Transfer (SCT):



Target image

Problem:

No control of the distribution of selected superpixels in the source image.







Transfer result (average colors)

Selected superpixels

Problem:

No control of the distribution of selected superpixels in the source image.

Solution:

To constrain a source superpixel to be selected no more than ϵ times.



- Optimal transport [Pitié et al., 2007]
 - Relaxed optimal transport [Rabin et al., 2014]
 - 3D color gamut mapping [Nguyen et al., 2014]



Target image



Source image



SCT



[Pitié et al., 2007]



Rabin et al., 2014



[Nguyen et al., 2014]

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Superpixel-based matches:

 \rightarrow No use of the neighborhood, loss of spatial consistency.





Optical flow representation



Superpixel-based matches:

 \rightarrow No use of the neighborhood, loss of spatial consistency.





Optical flow representation



Impact of the neighborhood

Usual distance between regular patches:



Sum of squared differences (patches of size $(2s+1)^2$):

$$D(P(p), P(q)) = \sum_{i=-s}^{s} \sum_{j=-s}^{s} \left(A(x+i, y+j) - B(x'+i, y'+j) \right)^{2}$$

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How to adapt to superpixels?

- Neighborhood structure preserving the geometry
- Comparison between two elements



• Definition:

All superpixels $A_{i'}$ with their barycenter $c_{i'}$ contained into a R radius.

 $\mathbf{A_i}$ superpatch of superpixel A_i : $\mathbf{A_i} = \{A_{i'}, \text{ such that } ||c_i - c_{i'}||_2 \le R\}$





Dissimilarity measure:
$$D(\mathbf{A_i}, \mathbf{B_j}) = \frac{\sum_{A_{i'} \in \mathbf{A_i}} \sum_{B_{j'} \in \mathbf{B_j}} w(A_{i'}, B_{j'}) d(F_{i'}^A, F_{j'}^B)}{A_{i'} \in \mathbf{A_i}} \sum_{B_{j'} \in \mathbf{B_j}} w(A_{i'}, B_{j'})}$$

Spatial weighting between registered barycenters:
$$w(A_{i'},B_{j'}) = \exp^{-\frac{\|c_{i'} - c_{j'} - v_{ij}\|_2^2}{\sigma^2}}$$





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Superpixel-based matches:

 \rightarrow Spatial consistency with the superpatch.





Optical flow representation

Application to segmentation and labeling

LFW dataset [Huang et al., 2007]:

1500 example images and 927 test images.

3 labels: hair, face and background.

Decompositions into superpixels provided.



Impact of the superpatch:





- Superpixels
- SPM (superpixels) (superpatches)

(superpixels)

SPM (superpatches)

Application to segmentation and labeling

• Impact of the superpatch:





• Comparison to state-of-the-art:

Method	Superpixel-wise	Pixel-wise
	accuracy	accuracy
Spatial CRF [Kae et al., 2013]	93.95%	×
CRBM [Kae et al., 2013]	94.10%	×
GLOC [Kae et al., 2013]	94.95%	×
DCNN [Liu et al., 2015]	×	95.24%
SuperPatchMatch (2016)	$\mathbf{95.08\%}$	$\mathbf{95.43\%}$

Conclusion

- PatchMatch for superpixels
- Constraint on the distribution of matches
- New superpixel neighborhood structure (superpatch)
- Competitive results with some learning-based methods

Associated publications:

- Rémi Giraud, Vinh-Thong Ta, Aurélie Bugeau, Pierrick Coupé, and Nicolas Papadakis. SuperPatchMatch: An algorithm for robust correspondences using superpixel patches. IEEE Trans. on Image Processing (TIP), 2017.
- <u>Rémi Giraud</u>, Vinh-Thong Ta, and Nicolas Papadakis. Transfert de couleurs basé superpixels. Actes du Groupe d'Études du Traitement du Signal et des Images (GRETSI), 2017.
- <u>Rémi Giraud</u>, Vinh-Thong Ta, and Nicolas Papadakis.
 Superpixel-based color transfer.
 Proc. of IEEE Interational Conference on Image Processing (ICIP), 2017.

• Impact of the superpixel decomposition \mathcal{S} :





Introduction

2 Matching algorithm based on patches for medical image segmentation

Matching algorithm based on patches of superpixels and applications

Decomposition into regular superpixels

- State-of-the-art
- The SCALP method
- Evaluation of regularity
- Results
- Conclusion



Simple Linear Iterative Clustering (SLIC) [Achanta et al., 2012]









Simple Linear Iterative Clustering (SLIC) [Achanta et al., 2012]







Distance between a pixel p and a superpixel S_k : $D(p, S_k) = d_{color}(F_p, F_{S_k}) + d_{spatial}(X_p, X_{S_k})m$



$$\begin{split} F_p &= [l_p, a_p, b_p] \text{ color in the CIELab space} \\ X_p &= [x_p, y_p] \text{ position} \\ F_{S_k}, X_{S_k} \text{ average on pixels} \in S_k \\ m \text{ regularity parameter} \end{split}$$
State-of-the-art - The SLIC method

Distance between a pixel p and a superpixel S_k :

$$D(p, S_k) = d_{color}(F_p, F_{S_k}) + d_{spatial}(X_p, X_{S_k})m$$

Limitations:

- Global regularity parameter \rightarrow irregular shapes with low m.
- No contour information \rightarrow low contour adherence performances.
- Only local pixel color considered \rightarrow no robustness to noise.





m = 60

m = 10

State-of-the-art - The SLIC method

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Initial image

Noisy image

Superpixels with Contour Adherence using Linear Path (SCALP):

- Color and contour distance on the linear path \mathbf{P}_p^k to the barycenter of the superpixel
- Color distance on the pixel neighborhood V(p)



The SCALP method

Superpixels with Contour Adherence using Linear Path (SCALP):

- Color and contour distance on the linear path \mathbf{P}_p^k to the barycenter of the superpixel
- Color distance on the pixel neighborhood V(p)



Color distance on linear path \mathbf{P}_p^k :

$$d_{\mathsf{path}}(\mathbf{P}_p^k, S_k) = \frac{1}{\left|\mathbf{P}_p^k\right|} \sum_{q \in \mathbf{P}_p^k} d_{\mathsf{color}}(F_q, F_{S_k})$$



Color distance on linear path \mathbf{P}_{p}^{k} :

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$$S_k^{\mathbf{P}_p^k}$$

ightarrow Prevents the appearance of irregular shapes by encouraging convexity.



Contour distance on linear path \mathbf{P}_p^k : $d_{\mathsf{contour}}(\mathbf{P}_p^k) = \gamma \max_{q \in \mathbf{P}_p^k} \mathcal{C}(q)$



 \rightarrow Possible use of a contour map ${\mathcal C}$ to favor the respect of image objects.

Contour distance on linear path \mathbf{P}_p^k : $d_{\text{contour}}(\mathbf{P}_p^k) = \gamma \max_{q \in \mathbf{P}_p^k} \mathcal{C}(q)$



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Image

Linear path

Max. contour

Result



 \rightarrow Possible use of a contour map ${\mathcal C}$ to favor the respect of image objects.



Color distance on the neighborhood V(p):

$$d_{\mathsf{neigh.}}(V(p),S_k) = \sum_{q \in V(p)} d_{\mathsf{color}}(F_q,F_{S_k}) w_{p,q}$$



The SCALP method - Pixel neighborhood

Color distance on the neighborhood V(p): $d_{\mathsf{neigh.}}(V(p),S_k) = \sum_{q \in V(p)} d_{\mathsf{color}}(F_q,F_{S_k}) w_{p,q}$



 \rightarrow Robustness to noise.



Image

Without neighborhood

With neighborhood

The SCALP method - Pixel neighborhood

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Image

Without neighborhood

With neighborhood

Final SLIC distance [Achanta et al., 2012]:

 $D(p, S_k) = d_{\text{color}}(F_p, F_{S_k}) + d_{\text{spatial}}(X_p, X_{S_k})m$

The SCALP method - Pixel neighborhood

Color distance on the neighborhood V(p): $d_{\mathsf{neigh.}}(V(p),S_k) = \sum_{q \in V(p)} d_{\mathsf{color}}(F_q,F_{S_k}) w_{p,q}$



 \rightarrow Robustness to noise.



Image

Without neighborhood

With neighborhood

Final distance SCALP: $D(p, S_k) = \left(d_{\mathsf{neigh.}}(V(p), S_k) + d_{\mathsf{path}}(\mathbf{P}_p^k, S_k) + d_{\mathsf{spatial}}(p, S_k)m \right) \left(1 + d_{\mathsf{contour}}(\mathbf{P}_p^k) \right)$



Image



ERS





ERGC







SCALP

Image



Image















Image

Results - Quantitative comparison to state-of-the-art

• Respect of image objects:







Image

Manual segmentation

Superpixels

- Achievable Segmentation Accuracy (ASA) [Liu et al., 2011] Superposition with the objects of the manual segmentation
- F-measure (F) [Martin et al., 2004]

Contour detection (Precision-Recall curves)

Results - Quantitative comparison to state-of-the-art

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Contour detection (Precision-Recall curves)

Validation on the BSD dataset: 200 images (321×481 pixels) [Martin et al., 2001]

Method	F	ASA
ERS [Liu et al., 2011]	0.593	0.951
SLIC [Achanta et al., 2012]	0.633	0.944
ERGC [Buyssens et al., 2014]	0.593	0.948
ETPS [Yao et al., 2015]	0.631	0.943
LSC [Chen et al., 2017]	0.607	0.950
SCALP	0.680	0.954

Results - Quantitative comparison to state-of-the-art

• Respect of image objects:







Image

Manual segmentation

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SLIC [Achanta et al., 2012]	0.633	0.944
ERGC [Buyssens et al., 2014]	0.593	0.948
ETPS [Yao et al., 2015]	0.631	0.943
LSC [Chen et al., 2017]	0.607	0.950
SCALP	0.680	0.954

- Regularity of the decomposition:
 - Circularity (C) [Schick et al., 2012] \rightarrow Limited evaluation metric

Reference measures in the literature:

Circularity (C) [Schick et al., 2012]: $C(S) = \frac{4\pi |S|}{|P(S)|^2}$

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Definition: a regular shape should be convex





Definition: a regular shape should be convex, with smooth contours



Definition: a regular shape should be convex, with smooth contours and balanced.



Definition: a regular shape should be convex, with smooth contours and balanced.



\rightarrow Equivalent measure for the square and circle

- \rightarrow Less sensitive to noise
- \rightarrow Robust to scale

Definition: a regular shape should be convex, with smooth contours and balanced.





0.870

0.712

0.410

0.474

0.580

0.564

0.440

0.500

 \rightarrow Less sensitive to noise

1.000

0.989

0.430

0.633

 \rightarrow Robust to scale

0.830

1.000

0.480

0.716

С

С

SRC

SRC

Definition: a regular shape should be convex, with smooth contours and balanced.



- \rightarrow Equivalent measure for the square and circle
- \rightarrow Less sensitive to noise
- \rightarrow Robust to scale

Definition: a regular shape should be convex, with smooth contours and balanced.



- \rightarrow Equivalent measure for the square and circle
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- Insufficient local evaluation
 - \rightarrow No taking into account of the consistency of shapes and sizes.





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SRC = 1.000	SRC = 1.000	

Evaluation of the superpixel shape consistency

Smooth Matching Factor (SMF): $SMF(S) = 1 - \sum_{S_k \in S} \frac{|S_k|}{|I|} \cdot \left\| \frac{S_k^*}{|S_k^*|} - \frac{S^*}{|S^*|} \right\|_1 / 2$



- Insufficient local evaluation
 - \rightarrow No taking into account of the consistency of shapes and sizes.

$\mathrm{SRC} = 1.000$	SRC = 1.000	

Evaluation of the superpixel shape consistency

$$\begin{split} & \text{Smooth Matching Factor (SMF):} \\ & \text{SMF}(\mathcal{S}) = 1 - \sum_{S_k \in \mathcal{S}} \frac{|S_k|}{|I|} \cdot \left\| \frac{S_k^*}{|S_k^*|} - \frac{S^*}{|S^*|} \right\|_1 / 2 \end{split}$$



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Evaluation of the superpixel shape consistency

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Global evaluation of regularity

Global Regularity (GR):
$$\mathrm{GR}(\mathcal{S}) = \mathrm{SMF}(\mathcal{S}) \sum_{S_k \in \mathcal{S}} \frac{|S_k|}{|I|} \mathrm{SRC}(S_k)$$

Validation on the standard BSD dataset [Martin et al., 2001]. 200 images (321×481 pixels) with manual segmentations.

- Respect of image objects
 - Superposition with several objects: ASA
 - Contour detection: F-measure
- Regularity of the decomposition
 - Regularity of shape and consistency: GR

Method	F	ASA	GR
ERS [Liu et al., 2011]	0.593	0.951	0.195
SLIC [Achanta et al., 2012]	0.633	0.944	0.336
ERGC [Buyssens et al., 2014]	0.593	0.948	0.235
ETPS [Yao et al., 2015]	0.631	0.943	0.494
LSC [Chen et al., 2017]	0.607	0.950	0.238
SCALP	0.680	0.954	0.391




Conclusion

- State-of-the-art results with high regularity
- Limited computational time
- Natural extension to supervoxels

Associated publications:

- <u>Rémi Giraud</u>, Vinh-Thong Ta, and Nicolas Papadakis.
 <u>SCALP: Superpixels with contour adherence using linear path</u>. Proc. of International Conference on Pattern Recognition (ICPR), pages 2374–2379, 2016.
- <u>Rémi Giraud</u>, Vinh-Thong Ta, and Nicolas Papadakis. Décomposition en superpixels via l'utilisation de chemin linéaire. Actes du Groupe d'Etudes du Traitement du Signal et des Images (GRETSI), 2017.
- Rémi Giraud, Vinh-Thong Ta, and Nicolas Papadakis. Robust shape regularity criteria for superpixel evaluation. Proc. of IEEE International Conference on Image Processing (ICIP), 2017.
- <u>Rémi Giraud</u>, Vinh-Thong Ta, and Nicolas Papadakis.
 <u>Evaluation framework of superpixel methods with a global regularity measure</u>.
 Journal of Electronic Imaging (JEI), 2017.
- <u>Rémi Giraud</u>, Vinh-Thong Ta, and Nicolas Papadakis. Robust superpixels using color and contour features along linear path. Computer Vision and Image Understanding (CVIU) (en révision), 2017.





Matching algorithm based on patches of superpixels and applications

4



Conclusion and perspectives

Conclusion

Context:

Non-local exemplar-based methods

- without learning
- large example datasets
- fast



- Synthesis of contributions:
 - 1) Low resolution descriptors:
 - \rightarrow SCALP, GR, Superpatch
 - 2) Matching algorithms:
 - \rightarrow OPAL, SuperPatchMatch, SCT
 - 3) Applications:
 - \rightarrow 3D Medical image segmentation
 - \rightarrow Alzheimer's disease detection
 - \rightarrow Color transfer between images
 - \rightarrow Superpixel-based segmentation and labeling
 - \rightarrow ...

- Supervoxel-based segmentation of 3D medical images
 - \rightarrow To adapt SuperPatchMatch for complex structures, *e.g.*, tumors:
 - No prior on position
 - Contours correlated to the MRI image content



Example of 2D segmentation of tumors on the BRATS dataset [Menze et al., 2015]

- Computer graphics (style transfer):
 - \rightarrow Important computational time
 - \rightarrow Copy of the same parts
 - \rightarrow Strict respect of contours



Target image



Source image



Patch-based [Frigo et al., 2016]



- Computer graphics (style transfer):
 - \rightarrow Important computational time
 - \rightarrow Copy of the same parts
 - \rightarrow Strict respect of contours



Target image



Source image



Patch-based [Frigo et al., 2016]



- Computer graphics (style transfer):
 - \rightarrow Important computational time
 - \rightarrow Copy of the same parts
 - \rightarrow Strict respect of contours



Target image



Source image



Patch-based [Frigo et al., 2016]

- \rightarrow Superpixels to reduce the computational cost
- \rightarrow Constraint search for matches (SCT)
- \rightarrow To force the capture of the image contours



Image

SCALP

inversed SCALP



Matching algorithms and superpixels for image analysis and processing

Thank you for your attention.

Questions?



Publications

- Vinh-Thong Ta, <u>Rémi Giraud</u>, D. Louis Collins, and Pierrick Coupé. Optimized PatchMatch for near real time and accurate label fusion. Proc. of Int. Conf. on Medical Image Computing and Computer-Assisted Intervention (MICCAI), pages 105–112, 2014.
- Memi Giraud, Vinh-Thong Ta, Nicolas Papadakis, D. Louis Collins, and Pierrick Coupé. Optimisation de l'algorithme PatchMatch pour la segmentation de structures anatomiques. Actes du Groupe d'Etudes du Traitement du Signal et des Images (GRETSI), 2015.
- Rémi Giraud, Vinh-Thong Ta, Nicolas Papadakis, José V. Manjón, D. Louis Collins, and Pierrick Coupé. An optimized PatchMatch for multi-scale and multi-feature label fusion. NeuroImage (NIMG), 124:770-782, 2016.
- Rémi Giraud, Vinh-Thong Ta, and Nicolas Papadakis. SCALP: Superpixels with contour adherence using linear path. Proc. of International Conference on Pattern Recognition (ICPR), pages 2374–2379, 2016.
- Kilian Hett, Vinh-Thong Ta, <u>Rémi Giraud</u>, Mary Mondino, José V. Manjón, and Pierrick Coupé. Patch-based DTI grading: Application to alzheimer's disease classification. Proc. of Int. Work. on Patch-based Techniques in Medical Imaging (Patch-MI, MICCAI), pages 76–83, 2016.
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Publications

- <u>Rémi Giraud</u>, Vinh-Thong Ta, and Nicolas Papadakis. Transfert de couleurs basé superpixels. Actes du Groupe d'Études du Traitement du Signal et des Images (GRETSI), 2017.
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 <u>Superpixel-based color transfer</u>.
 Proc. of IEEE International Conference on Image Processing (ICIP), 2017.
- Rémi Giraud, Vinh-Thong Ta, and Nicolas Papadakis. Robust shape regularity criteria for superpixel evaluation. Proc. of IEEE International Conference on Image Processing (ICIP), 2017.
- <u>Rémi Giraud</u>, Vinh-Thong Ta, and Nicolas Papadakis.
 <u>Evaluation framework of superpixel methods with a global regularity measure</u>. Journal of Electronic Imaging (JEI), 2017.
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- <u>Rémi Giraud</u>, Vinh-Thong Ta, and Nicolas Papadakis. Robust superpixels using color and contour features along linear path. Computer Vision and Image Understanding (CVIU) (en révision), 2017.

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Annex

Matching algorithm based on patches for medical image segmentation

The PatchMatch algorithm

Reconstruction of an image A from the selected patches in an image B



 $\mathsf{Image}\ B$



Image \tilde{A} (exhaustive search) (t=10h)



Image \tilde{A} [Barnes et al., 2009] (t=14s)

The PatchMatch algorithm

Coherency Sensitive Hashing [Korman and Avidan, 2011, Korman and Avidan, 2016]

Idea: To use a patch-based hash table to facilitate the search for matches.

 \rightarrow Necessity to have the input image to compute the hashing of example images.



The OPAL method - Label fusion

S subject to segment,

 $T = \{T_1, \ldots, T_n\}_{n=1,\ldots N}$ the N example models, $P(\mathbf{x_i}) \in S$ the 3D patch at the position $\mathbf{x_i} = (x, y, z) \in S$, $\mathcal{K}_i = \{\mathbf{x_{j,t}}\}$ the set of positions of selected patches,

 $l(\mathbf{x_{j,t}})$ the label (0 or 1) given by the expert at voxel $\mathbf{x_{j,t}}$,

Label fusion:

$$\mathcal{L}(P(\mathbf{x_i})) = \frac{\sum_{\mathbf{x_{j,t} \in \mathcal{K}_i}} \omega\left(\mathbf{x_i}, \mathbf{x_{j,t}}\right) L\left(P(\mathbf{x_{j,t}})\right)}{\sum_{\mathbf{x_{j,t} \in \mathcal{K}_i}} \omega\left(\mathbf{x_i}, \mathbf{x_{j,t}}\right)} \qquad \qquad \mathcal{S}(\mathbf{x_i}) = \begin{cases} 1, & \text{if } \mathcal{L}(\mathbf{x_i}) \ge 0.5\\ 0, & \text{otherwise} \end{cases}$$

Comparison of patches:

$$\begin{split} \omega(\mathbf{x_i}, \mathbf{x_{j,t}}) &= \exp\left(1 - \left(\frac{\|P(\mathbf{x_i}) - P(\mathbf{x_{j,t}})\|_2^2}{h(\mathbf{x_i})^2} + \frac{\|\mathbf{x_i} - \mathbf{x_j}\|_2}{\sigma^2}\right)\right) \\ h(\mathbf{x_i})^2 &= \alpha^2 \min_{\mathbf{x_{j,t}} \in \mathcal{K}_i} (\|P(\mathbf{x_i}) - P(\mathbf{x_{j,t}})\|_2^2 + \epsilon) \end{split}$$

The OPAL method - Impact of parameters

Impact of the initialization window size

 \rightarrow Set by default at $13{\times}13{\times}13$ voxels



Very limited computational time

\rightarrow Independent multi-feature and multi-scale search and fusion



Dataset	Multi-feature	Multi-scale	Median Dice	Average Dice	p-value	Computational time
ICBM	×	×	89.4%	$89.1 \pm 1.85\%$	$< 10^{-14}$	0.27s
	1	×	89.8%	$89.6 \pm 1.68\%$	0.0131	0.53s
	1	1	89.9%	$89.7 \pm 1.70\%$	×	0.92s
EADC-ADNI	×	×	89.4%	$89.2 \pm 1.55\%$	$< 10^{-25}$	0.49s
	1	×	89.7%	$89.6 \pm 1.45\%$	$< 10^{-8}$	0.95s
	1	1	90.1%	$89.8\pm1.46\%$	×	1.48s

Very limited computational time

 \rightarrow Independent multi-feature and multi-scale search and fusion



Segmentation

Very limited computational time

 \rightarrow Independent multi-feature and multi-scale search and fusion



The OPAL method - Results

 $\begin{aligned} & \text{Validation metric [Zijdenbos et al., 1994]:} \\ & \text{Dice}(\mathcal{S}_{\text{expert}}, \mathcal{S}_{\text{auto}}) = \frac{2|\mathcal{S}_{\text{expert}} \cap \mathcal{S}_{\text{auto}}|}{|\mathcal{S}_{\text{expert}}| + |\mathcal{S}_{\text{auto}}|} \end{aligned}$

• ICBM dataset: 80 young healthy subjects [Mazziotta et al., 1995] Inter-expert variability: 90%.

Method	Median Dice	Computational time
Patch-based [Coupé et al., 2011]	$88.2 \pm 2.19\%$	$(\times 700)$
Multi-templates [Collins and Pruessner, 2010]	$88.6 \pm 2.05\%$	$(\times 4300)$
Sparse coding [Tong et al., 2013]	$88.7 \pm 1.94\%$	(×6000)
Dictionary learning [Tong et al., 2013]	$89.0 \pm 1.90\%$	$(\times 1000)$
OPAL (2015)	$90.0 \pm \mathbf{1.70\%}$	0.92s

• EADC-ADNI: 100 healthy and unhealthy subjects [Boccardi et al., 2014] Inter-expert variability: 89%.

Method	Average Dice	Computational time
Random Forest [Tangaro et al., 2014]	$76.0 \pm 7.00\%$	×
Multi-templates [Roche et al., 2014]	$86.6 \pm 1.70\%$	×
Multi-templates Gray et al., 2014	$87.6 \pm 2.07\%$	×
Patch-based [Zhu et al., 2017]	$88.3 \pm 2.50\%$	×
Multi-scale patch-based [Pant et al., 2015]	$89.2 \pm 2.22\%$	$(\times 200)$
OPAL (2015)	$89.8 \pm 1.46\%$	1.48s

The OPAL method - Adding subjects to the library

The complexity of OPAL only depends on the subject size: \rightarrow Adding automatically segmented subjects to the library



The OPAL method - Application to cerebellum segmentation

Several complex and adjacent structures

 \rightarrow Weighting and regularization of estimator maps [Romero et al., 2017]

Comparison to MAGET [Park et al., 2014] and RASCAL [Weier et al., 2014] Computational time: MAGET (2h), RASCAL (4h), CERES (1mn)





Structure	MAGeT	RASCAL	CERES	Intra-expert
Lobule I-II	0.3960 ± 0.1424	0.3260 ± 0.2178	0.5201 ± 0.1555	0.639
Lobule III	0.6800 ± 0.1741	0.6379 ± 0.2165	0.7213 ± 0.1572	0.751
Lobule IV	0.6980 ± 0.1440	0.6627 ± 0.1611	0.7271 ± 0.1346	0.818
Lobule V	0.7320 ± 0.1398	0.6666 ± 0.1560	0.7561 ± 0.1332	0.881
Lobule VI	0.8710 ± 0.0359	0.7969 ± 0.0523	0.8695 ± 0.0316	0.912
Lobule Crus I	0.8870 ± 0.0257	0.8383 ± 0.0351	0.9007 ± 0.0152	0.904
Lobule Crus II	0.7780 ± 0.0679	0.7340 ± 0.0667	0.8096 ± 0.0569	0.900
Lobule VIIB	0.5990 ± 0.1487	0.5820 ± 0.1137	0.6850 ± 0.1205	0.863
Lobule VIIIA	0.7300 ± 0.0934	0.6757 ± 0.1426	0.7926 ± 0.0759	0.860
Lobule VIIIB	0.7970 ± 0.0607	0.7783 ± 0.0931	0.8533 ± 0.0390	0.833
Lobule IX	0.8560 ± 0.0384	0.8460 ± 0.0545	0.8849 ± 0.0327	0.874
Lobule X	0.7540 ± 0.0490	0.7237 ± 0.0680	0.7548 ± 0.0469	0.760
Cerebellum	0.9250 ± 0.0094	0.9349 ± 0.0089	0.9377 ± 0.0090	0.941
Average	0.7320 ± 0.0568	0.6890 ± 0.0524	0.7729 ± 0.0427	0.833

The OPAL method - Application to Alzheimer's disease prediction

Automatic classification using OPAL for the search of matches. Label fusion of the pathologies of the library models.

(NC = Normal Controls, AD = Alzheimer Disease, MCI = Mild Cognitive Impairment)



Classification performances on several features.

	Features	NC vs AD	NC vs MCI	AD vs MCI	eMCI vs IMCI
	Volume	88.4/83.1	69.5/63.9	71.1/67.2	67.2/63.7
	FA	64.2/59.2	57.7/56.1	54.0/52.7	38.2/43.1
Average	MD	85.7/80.3	66.0/62.6	75.0/72.5	67.6/62.8
	AxD	83.5/81.4	63.5/58.0	74.3/70.2	68.9/66.8
	RD	86.2/79.2	66.5/62.3	74.8/70.5	66.0/61.5
	T1	93.4/87.8	71.3/64.1	82.0/73.4	68.7/66.2
	FA	85.0/80.1	63.5/60.1	74.9/70.3	63.0/60.7
OPAL	MD	90.6/86.5	68.8/60.7	80.4/76.3	70.4/65.8
	AxD	91.1/85.8	68.7/59.6	80.2/73.1	71.8/67.6
	RD	90.3/85.1	68.9/61.0	80.0/76.5	69.3/65.4

The OPAL method - volBrain

Integration of OPAL to the volBrain platform [Manjón and Coupé, 2016] (http://volbrain.upv.es)

- Online volumetric study system of cerebral MRI images
- Detailed reports (tissues, white matter, hippocampus, etc.) with segmentation files
- Since mars 2015, more than 1400 users across the world for more than 45000 processed MRI images



volBrain Volumetry Report writer 1.0 million 04-03-2015 Sex Male Report Date 03-Sep-2015 Tissue type White Matter (WM) Volume (cm²/%) 632.15 (38.99%) Grey Matter (GM) [43.84, 55.11] 0.88 Canbro Spinal Fluid (CSF) Cerebram Total (cm³/5.) Right (cm²/%) Left (cm²/%) Aqm.(%) WM WM 648.56 530.65 (40.005) (15.185) 324.56 284.60 (20.02%) (17.55%) 324.01 286.05 (19.985) (17.645) Carabalam Total (cm³/%) Right (cm²7%) 28.16 (4.82%) Aoym.(%) -4.2525 18.54.11.091 WM GM GM (1667) (1607) (1777) [244, 424] [8.46, 128] Brainsten Total (cm²/%) 28.16(1.74%)(1.49, 1.99) Total scn¹/5 Richt (cm²/5) Latt (cm²/Fr) Avanativ (5) (0.47%) 7,67 (0.47%) 4.1648 (A 118, 6.6) -6.7293 13.17(0.815) (425.435) 6.55 (0.40%) 0.9995 (0.11, 6×11) 2,992-00 (1955) 1.44.01.0955 p.36, 0.27) 1 51 JB (1975.) 1.5640 (0.10) 1.79 (0.30%) pat, a 11] 4.66 (0.29%) 9.45(0.585) In processo 2.6568 (-0.1566) 12.44[-6.1667









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Annex

Matching algorithm based on patches of superpixels and applications

Adaptation of PatchMatch propagation step



Selection of the neighbor with the most similar orientation:

$$C_{(i')} = \underset{k \in \mathcal{N}_{\mathcal{M}(i')}^{B}}{\operatorname{argmin}} \|(\theta_{ii'} + \pi) - \theta_{i'k}\|_{1}$$







The SCT method - Previous works



- Parametric methods: statistics transfer. Reinhard et al., 2001, Tai et al., 2005
 - \rightarrow No guarantee to have a relevant color transfer.
- Optimal transport (OT): transfer of color histogram. Pitié et al., 2007, Rabin et al., 2012, Frigo et al., 2014
 - \rightarrow The exact transfer may lead to visual outliers.
- Relaxed OT: adaptive transfer of the source colors using superpixels. [Rabin et al., 2014]
 - \rightarrow High computational cost with OT methods.



Reinhard et al., 2001



Pitié et al., 2007


The SCT method - Global matching of superpixels

Proposed solution: A superpixel in B cannot be selected more than ϵ times.

If a superpixel A_i finds a better match B_k already taken by ϵ superpixels $A_j?$ Switch between matches:



 \rightarrow Optimization of the total matching distance $\sum_i D(A_i, B_{(i)})$.

The SCT method - Global matching of superpixels

 \rightarrow With the constraint set by ϵ_{r} global selection of the source color palette.



The SCT method - Global assignment problem

With $\epsilon = 1$, approximation of the optimal assignment problem: "Given two sets $A = \{A_i\}_{i \in \{1,...,|A|\}}$ and $B = \{B_j\}_{j \in \{1,...,|B|\}}$ with $|A| \leq |B|$, association of each A_i to a unique $B_{(i)}$ that minimizes $\sum_i D(A_i, B_{(i)})$."

Problem addressed with costly optimal algorithms [Munkres, 1957]



 \rightarrow Close results to the optimal resolution in very reduced computational time.

• Fusion of selected colors by non-local means [Buades et al., 2005]:

Superpixel $A_i = [X_i, C_i] = [(x_i, y_i), (r_i, g_i, b_i)].$

For all pixels $p \in A_i$, contribution of superpixels A_j .



 \rightarrow Only transfer existing source colors.

• Weighting based on spatial and color similarity:

Distance using covariance information of A_i : $\omega(p, A_j) = \exp\left(-(p - \bar{A}_j)^T Q_i^{-1}(p - \bar{A}_j)\right)$

 \rightarrow Respect of the target image structures.

The SCT method - Step summary

Total computational time < 1s (480×360 pixels).



Target image

Source image



Superpixels

Transfer of average colors

Final result

The SCT method - Influence of the matching constraint

With the constraint set by ϵ , homogeneous selection of the source superpixels. \rightarrow Global transfer of the source color palette.



Source image

Selection map

Selection map

The SCT method - Influence of the matching constraint

With the constraint set by ϵ , homogeneous selection of the source superpixels. \rightarrow Global transfer of the source color palette.



Target image



SCT ($\epsilon = \infty$)

Transfer result

SCT ($\epsilon = 3$)



Transfer result



Source image



Selection map



Selection map

- Optimal transport [Pitié et al., 2007]
 - Relaxed optimal transport [Rabin et al., 2014]
 - 3D color gamut mapping [Nguyen et al., 2014]



Target image



Source image



SCT



[Pitié et al., 2007]



[Rabin et al., 2014]



[Nguyen et al., 2014]

- Optimal transport [Pitié et al., 2007]
 - Relaxed optimal transport [Rabin et al., 2014]
 - 3D color gamut mapping [Nguyen et al., 2014]



Target image



Source image



SCT



[Pitié et al., 2007]



[Rabin et al., 2014]



[Nguyen et al., 2014]

- Optimal transport [Pitié et al., 2007]
 - Relaxed optimal transport [Rabin et al., 2014]
 - 3D color gamut mapping [Nguyen et al., 2014]



Target image



Source image



SCT



[Pitié et al., 2007]



[Rabin et al., 2014]



[Nguyen et al., 2014]

- Optimal transport [Pitié et al., 2007]
 - Relaxed optimal transport [Rabin et al., 2014]
 - 3D color gamut mapping [Nguyen et al., 2014]



Target image



Source image



SCT



[Pitié et al., 2007]



[Rabin et al., 2014]



[Nguyen et al., 2014]

- Optimal transport [Pitié et al., 2007]
 - Relaxed optimal transport [Rabin et al., 2014]
 - 3D color gamut mapping [Nguyen et al., 2014]



Target image



Source image



SCT



[Pitié et al., 2007]



[Rabin et al., 2014]



[Nguyen et al., 2014]

The SCT method - Several source images



Target image



Source images



SCT



[Pitié et al., 2007]



[Rabin et al., 2014]



[Nguyen et al., 2014]





Optical flow representation



Optical flow representation

Optical flow representation

SuperPatchMatch - Label fusion

Label fusion:

$$\begin{split} L_m(A_i) &= \frac{\sum_{T_j \in \mathcal{K}_i^m} \omega(A_i, T_j)}{\sum_{m=1}^M \sum_{T_j \in \mathcal{K}_i^m} \omega(A_i, T_j)} \\ \omega(A_i, T_j) &= \exp\left(1 - \left(\frac{D(\mathbf{A}_i, \mathbf{T}_j)}{h(A_i)^2} + \frac{\|c_i - c_j\|_2}{\beta^2}\right)\right) \\ \mathcal{L}(A_i) &= \operatorname*{argmax}_{m \in \{1, \dots, M\}} L_m(A_i) \end{split}$$

Superpixels A_i (test), T_j (library) $\mathcal{K}_i^m = \{T_i\}$ selected, with label m

Measure D between superpatches A_i and T_i c_i barycenter of superpixel A_i $h(A_i)$ minimal distance among the $D(A_i, T_i)$

97.60%

Superpixels

Ground truth

Face

Background Labeling probabilities L_m

Result \mathcal{L}

SuperPatchMatch - Impact of parameters

SuperPatchMatch - Impact of parameters

Adaptation of PatchMatch propagation step $(94.20\% \rightarrow 95.08\%)$

Ground truth

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• Comparison to state-of-the-art:

Method	Superpixel-wise	Pixel-wise	Computational
	accuracy	accuracy	time
PatchMatch (9×9)	87.73%	87.02%	3.940s
Spatial CRF [Kae et al., 2013]	93.95%	×	×
CRBM [Kae et al., 2013]	94.10%	×	×
GLOC [Kae et al., 2013]	94.95%	×	0.323s
DCNN [Liu et al., 2015]	×	95.24%	×
SuperPatchMatch (2016)	$\mathbf{95.08\%}$	95.43 %	0.255s

 \rightarrow Similar results to learning-based approaches

• Impact of regularity:

Annex

Decomposition into regular superpixels

Use of superpixels

Advantages of superpixels:

- Reduce the number of considered elements
- Robustness to noise
- Respect of image objects contours

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Limitations:

- $\bullet~\mbox{Shape}$ irregularity $\rightarrow~\mbox{Irregularity}$ of the neighborhood
 - \rightarrow Need for regular superpixels

Decomposition into superpixels

Adjacency graph

The SCALP method - Summary of equations

Color distance on the neighborhood:

$$\begin{split} d_{\text{neigh.}}(V(p),S_k) &= \sum_{q \in V(p)} d_{\text{color}}(F_q,F_{S_k}) w_{p,q} \\ w_{p,q} &= \frac{1}{Z} \exp\left(-\frac{d_{\text{color}}(F_q,F_{S_k})}{\sigma^2}\right) \end{split}$$

Color distance on linear path:

$$d_{\text{contour}}(\mathbf{P}_p^k) = 1 + \gamma \max_{q \in \mathbf{P}_p^k} \mathcal{C}(q)$$

Total color distance:

$$D_{\text{couleur}}(V(p), S_k, \mathbf{P}_p^k) \!=\! \lambda d_{\text{neigh.}}(V(p), S_k) + (1 - \lambda) \frac{1}{|\mathbf{P}_p^k|} \sum_{q \in \mathbf{P}_p^k} \! d_{\text{color}}(q, S_k)$$

Final distance:

$$D(p, S_k) = \left(D_{\text{color}}(V(p), S_k, \mathbf{P}_p^k) + d_{\text{spatial}}(X_p, X_{S_k})m \right) d_{\text{contour}}(\mathbf{P}_p^k)$$

The distance $d_{\text{neigh.}}$ on the neighborhood V(p) of pixel p can be computed in $\mathcal{O}(1)$.

Demonstration:

The distance between features F in $d_{\text{neigh.}}$ reads:

$$\begin{split} d_{\mathsf{neigh.}}(V(p),S_k) &= \sum_{q \in V(p)} (F_q - F_{S_k})^2 w_{p,q}, \\ &= \sum_{q \in V(p)} \left(F_q^2 + F_{S_k}^2 - 2F_q F_{S_k} \right) w_{p,q}, \\ &= \sum_{q \in V(p)} F_q^2 w_{p,q} + \sum_{q \in V(p)} F_{S_k}^2 w_{p,q} - 2 \sum_{q \in V(p)} F_q F_{S_k} w_{p,q}, \\ &= \mathcal{F}_p^{(2)} + F_{S_k}^2 \sum_{q \in V(p)} w_{p,q} - 2F_{S_k} \sum_{q \in V(p)} F_q w_{p,q}, \\ &= \mathcal{F}_p^{(2)} + F_{S_k}^2 - 2F_{S_k} \mathcal{F}_p^{(1)}. \end{split}$$

 $\mathcal{F}_p^{(2)} = \sum_{q \in V(p)} F_q^2$, and $\mathcal{F}_p^{(1)} = \sum_{q \in V(p)} F_q$, can be pre-computed. The complexity of $d_{\mathsf{neigh.}}$ is hence reduced to $\mathcal{O}(1)$ instead of $\mathcal{O}(N)$.

The SCALP method - Linear path definition

Path between a pixel p at position X_p and a superpixel S_k of barycenter X_{S_k} Real-time computation with the [Bresenham, 1965] algorithm

The SCALP method - Comparison to geodesic distances

Sinuous path with geodesics \rightarrow more irregular superpixels

Image

Geodesic distance

Linear path distance

[Rubio et al., 2016] (geodesic)

SCALP (linear path)

SCALP(I, K, C)

- 1: Initialization of features $S_k \leftarrow [F_{S_k}, X_{S_k}]$ from a regular grid
- 2: Initialization of superpixel labels $\tilde{\mathcal{S}} \stackrel{k}{\leftarrow} 0$
- 3: Pre-computation of features $\mathcal{F}_p^{(2)}$ and $\mathcal{F}_p^{(1)}$
- 4. For each iteration do
- 5: Distance $d \leftarrow \infty$
- 6: For each S_k do
- 7. For each pixel p in a $(2r+1) \times (2r+1)$ window centered on $X_{S_{l_{0}}}$ do
- Computation of the linear path \mathbf{P}_{n}^{k} [Bresenham, 1965] 8:
- Computation of $D(p, S_k)$ using \mathcal{C} and \mathbf{P}_n^k 9:
- If $D(p, S_k) < d(p)$ then 10: $d(p) \leftarrow D(p, S_k)$
- 11:
- $S(p) \leftarrow k$ 12:
- 13: For each S_k do
- 14: Update $[F_{S_{k}}, X_{S_{k}}]$
- 15: Return S

The SCALP method - Influence of parameters

Distance parameters

Neighborhood $|V(p)|=(2n+1)^2,$ λ color distance, γ contour distance

lnitial image $n=0, \lambda=1, \gamma=0$

 $n=3, \lambda=0.5, \gamma=0$

 $n=3, \lambda=0.5, \gamma=50$

contour distance

neighborhood

color distance

The SCALP method - Influence of parameters

Distance parameters

Neighborhood $|V(p)| = (2n+1)^2$, λ color distance, γ contour distance

Contour detection

Even a simple contour detection from the superpixel boundaries obtained at multiple scales improves the performances.

Hard constraint on the initial segmentation

Hierarchical segmentation from a contour map [Arbelaez et al., 2009] Thresholding of the segmentation by a parameter τ

The SCALP method - Initial segmentation constraint

Adaptation of the hierarchical segmentation to the superpixel scale

Initial images of the BSD



SCALP



SCALP+HC



SEEDS [Van den Bergh et al., 2012] and WP [Machairas et al., 2015] added to the comparison

The SCALP method - Initial segmentation constraint

Initial images of the BSD + Gaussian noise



SCALP



SCALP+HC



SEEDS [Van den Bergh et al., 2012] and WP [Machairas et al., 2015] added to the comparison

The SCALP method - Results



Image



ERS



ERGC



Image





ETPS

LSC

LSC

SCALP

SCALP



Image











Image

The SCALP method - Results



Image / Noisy image

The SCALP method - Results



Image / Noisy image



LSC



The SCALP method - Results on noisy images



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The SCALP method - Extension to supervoxels

Natural extension to supervoxels for the decomposition of 3D objects

Results on the BRATS dataset [Menze et al., 2015] (MRI with tumors)

ASA 3D: • SLIC 0.9840 [Achanta et al., 2012]

- ERCG 0.9652 [Buyssens et al., 2014]
- SCALP 0.9848



Image

Ground truth

Supervoxels

Image

Ground truth

Supervoxels

Regularity metrics - Compromise between the metrics

The metrics cannot be simultaneously optimized.



Superpixel metrics

Segmentation into superpixels $\mathcal S,$ ground truth segmentation $\mathcal G$

Global Regularity (GR): Shape regularity and consistency of superpixels

$$\begin{split} &\mathsf{SRC}(\mathcal{S}) = \sum_{k} \frac{|S_k|}{|I|} \cdot \frac{|S|}{|H_S|} \cdot \frac{|\mathsf{P}(H_S)|}{|\mathsf{P}(S)|} \cdot \frac{\min(\sigma_x, \sigma_y)}{\max(\sigma_x, \sigma_y)} \\ &\mathsf{SMF}(\mathcal{S}) = 1 - \sum_{S_k} \frac{|S_k|}{|I|} \cdot \left\| \frac{S^*}{|S^*|} - \frac{S_k^*}{|S_k^*|} \right\|_1 /2 \\ &\mathsf{GR}(\mathcal{S}) = \mathsf{SRC}(\mathcal{S})\mathsf{SMF}(\mathcal{S}) \end{split}$$

Precision-Recall (PR): Average of superpixels boundaries at multiple scales [Martin et al., 2004]

$$\mathsf{BR}(\mathcal{S},\mathcal{G}) = \frac{|\mathcal{B}(\mathcal{S}) \cap \mathcal{B}(\mathcal{G})|}{|\mathcal{B}(\mathcal{G})|} \qquad \mathsf{P}(\mathcal{S},\mathcal{G}) = \frac{|\mathcal{B}(\mathcal{S}) \cap \mathcal{B}(\mathcal{G})|}{|\mathcal{B}(\mathcal{S})|} \qquad \mathsf{F} = \frac{2.\mathsf{P.BR}}{\mathsf{P} + \mathsf{BR}}$$

Achievable Segmentation Accuracy (ASA): Respect of the image objects [Liu et al., 2011]

$$\mathsf{ASA}(\mathcal{S},\mathcal{G}) = \frac{1}{|I|} \sum_{k} \max_{i} |S_k \cap G_i|$$

Contour Density vs Boundary Recall (CD vs BR): Adherence to contours [Martin et al., 2004]

$$\mathsf{CD}(\mathcal{S}) = \frac{|\mathcal{B}(\mathcal{S})|}{|I|} \quad \mathsf{BR}(\mathcal{S}, \mathcal{G}) = \frac{|\mathcal{B}(\mathcal{S}) \cap \mathcal{B}(\mathcal{G})|}{|\mathcal{B}(\mathcal{G})|}$$

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Superpixels metrics - CD vs BR



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Segmentation into superpixels ${\mathcal S}$

E

Intra-Cluster Variation (ICV): [Benesova and Kottman, 2014] $\mathsf{ICV}(\mathcal{S}) = \frac{1}{|\mathcal{S}|} \sum_{S_k} \frac{1}{|S_k|} \sqrt{\sum_{p \in S_k} (I(p) - \mu(S_k))^2}$

Explained Variation (EV): [Moore et al., 2008]

$$EV(S) = \frac{\sum_{S_k} |S_k| (\mu(S_k) - \mu(I))^2}{\sum_{p \in I} (I(p) - \mu(I))^2} = 1 - \sum_{S_k} \frac{|S_k|}{|I|} \cdot \frac{\sigma(S_k)^2}{\sigma(I)^2}$$



Segmentation into superpixels $\ensuremath{\mathcal{S}}$

Intra-Cluster Variation (ICV): [Benesova and Kottman, 2014] $\mathsf{ICV}(\mathcal{S}) = \frac{1}{|\mathcal{S}|} \sum_{S_k} \frac{1}{|S_k|} \sqrt{\sum_{p \in S_k} (I(p) - \mu(S_k))^2}$

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Segmentation into superpixels ${\mathcal S}$

Intra-Cluster Variation (ICV): [Benesova and Kottman, 2014]

$$\mathsf{ICV}(\mathcal{S}) = \frac{1}{|\mathcal{S}|} \sum_{S_k} \frac{1}{|S_k|} \sqrt{\sum_{p \in S_k} (I(p) - \mu(S_k))^2}$$

Explained Variation (EV): [Moore et al., 2008]

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• Shape regularity





Robustness to noise

SLIC superpixels with noise on the boundaries



m = 10

m = 50

m = 200

Robustness to noise

SLIC superpixels with noise on the boundaries



Evolution of the regularity parameter m Average results on the BSD



• Evaluation of the superpixel decomposition consistency



 \rightarrow Does not consider the size of superpixels. Thresholding not robust to large superpixels.

Smooth Matching Factor (SMF):

$$SMF(S) = 1 - \sum_{S_k} \frac{|S_k|}{|I|} \cdot \left\| \frac{S_k^*}{|S_k^*|} - \frac{S^*}{|S^*|} \right\|_1 / 2$$

 \rightarrow Direct comparison to the average shape S^* \rightarrow More relevant and robust metric







 $\mathsf{SMF} = 0.517$

• Global evaluation of the regularity: shape and consistency

Global Regularity (GR):
$$\mathsf{GR}(\mathcal{S}) = \mathsf{SMF}(\mathcal{S}) \sum_{S_k \in \mathcal{S}} \frac{|S_k|}{|I|} \mathsf{SRC}(S_k)$$

- \rightarrow SCALP generates very regular superpixels while respecting the image contours.
- \rightarrow The evaluation of performances at several regularity levels enables to be robust to the choice of the regularity parameter and to better represent a superpixel method potential.



The regularity of superpixels facilitates the tracking of objects.



Tracking accuracy with the TSP method [Chang et al., 2013] on the sequences from [Tsai et al., 2012].

	Acc	uracy	Loss		
Sequence	Regular	Irregular	Regular	Irregular	
birdfall2	98.3%	97.8%	1.0%	1.4%	
girl	51.1%	50.4%	13.9%	24.8%	
parachute	75.3%	73.9%	4.5%	5.1%	
penguin	94.3%	85.0%	2.6%	8.8%	
Average	79.8%	76.7%	5.5%	10.0%	



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penguin	94.3%	85.0%	2.6%	8.8%	
Average	79.8%	76.7%	5.5%	10.0%	



The irregularity facilitate the approximation of the initial colors. Colors contained into a superpixel approached by a third order polynomial.



Initial image I

Regular compression I_r

Irregular compression I_r

Average on the BSD images [Martin et al., 2001]



The regularity is correlated to performances.



The fusion of irregular decompositions may enable to efficiently segment the image objects.





Higher correlation between the proposed metrics and the performances.

	GR	SMF	J	SRC	С
ASA	-0.5473	-0.5250	-0.5266	-0.5350	-0.5318
UE	0.5506	0.5284	0.5299	0.5384	0.5353
BR	-0.9136	-0.8974	-0.8972	-0.9049	-0.9034
Р	-0.9627	-0.9645	-0.9656	-0.9688	-0.9712
EV	-0.6641	-0.6426	-0.6428	-0.6528	-0.6503
MSE	0.6760	0.6552	0.6554	0.6655	0.6636
Average	0.8165	0.8113	0.8076	0.8122	0.8085

Annex

Perspectives

Perspectives - Synthesis of non-linear transformation

 \rightarrow To adapt OPAL to the transfer of displacement vectors



Smart fusion of displacement vectors:



Previous works:

Smart fusion of optical flow vectors [Fortun et al., 2016] Patch-based synthesis of non-linear transformations [Kim et al., 2015]

Perspectives - Supervoxel-based segmentation of medical images

- Supervoxel-based segmentation of 3D medical images
 - \rightarrow To adapt SuperPatchMatch for complex structures, *e.g.*, tumors:
 - No prior on tumor position
 - Contours correlated to the MRI image content



Example of 2D segmentation of tumors on the BRATS dataset [Menze et al., 2015]

Perspectives - Style transfer

Patch-based method [Frigo et al., 2016]:









Result

- \rightarrow Important computational time
- \rightarrow Copy of the same image parts
- \rightarrow Transfer of texture and colors = too strict respect of the target contours
- \rightarrow Superpixels to reduce the computational cost
- \rightarrow Constrained search for matches (SCT)
- \rightarrow To force the capture of the image contours

Distance *inversed* SCALP:

$$D(p, S_k) = \left(d_{\text{spatial}}(p, S_k)m - D_c(V(p), S_k, \mathbf{P}_p^k) \right) \frac{1}{d_{\text{contour}}(\mathbf{P}_k^k)}$$



inversed SCALP

Perspectives - Style transfer

Comparison to neural network:



Target image

Source image



Patch-based method [Frigo et al., 2016]



Neural network [Gatys et al., 2015]